



# Cambridge International AS & A Level

CANDIDATE  
NAME

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CENTRE  
NUMBER

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**MATHEMATICS**

**9709/31**

Paper 3 Pure Mathematics 3

**October/November 2022**

**1 hour 50 minutes**

You must answer on the question paper.

You will need: List of formulae (MF19)

## INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

## INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **20** pages. Any blank pages are indicated.

1 (a) Sketch the graph of  $y = |2x + 1|$ .

[1]

(b) Solve the inequality  $3x + 5 < |2x + 1|$ .

[3]

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- 2 On a sketch of an Argand diagram shade the region whose points represent complex numbers  $z$  satisfying the inequalities  $|z| \leq 3$ ,  $\operatorname{Re} z \geq -2$  and  $\frac{1}{4}\pi \leq \arg z \leq \pi$ . [4]















(b) Verify by calculation that  $a$  lies between 0.9 and 1. [2]

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(c) Use an iterative formula based on the equation in part (a) to determine  $a$  correct to 2 decimal places. Give the result of each iteration to 4 decimal places. [3]

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(b) Given that  $x = 40$  when  $t = 10$ , find the value of  $k$  and find the value approached by  $x$  as  $t$  becomes large. [3]

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- (b) Calculate the angle in degrees between the directions of  $\overrightarrow{MD}$  and  $\overrightarrow{ON}$ . [3]

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- (c) Show that the length of the perpendicular from  $M$  to  $ON$  is  $\sqrt{\frac{22}{5}}$ . [4]

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