

Cambridge International AS & A Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

MATHEMATICS 9709/63

Paper 6 Probability & Statistics 2

October/November 2022

1 hour 15 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

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spin		
a)	Use a binomial distribution to carry out the test at the 5% significance level.	[5]
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an	jay also spins the spinner 40 times. He finds that it lands on red r times.	
	jay also spins the spinner 40 times. He finds that it lands on red r times. Use a binomial distribution to find the largest value of r that lies in the rejection region for test at the 5% significance level.	r the
	Use a binomial distribution to find the largest value of r that lies in the rejection region for	
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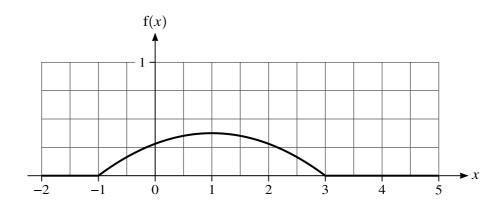
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	Find the probability that at least 3 drops fall during a randomly chosen 30-second period. [3
)	Use a suitable approximating distribution to find the probability that at least 650 drops fall during a randomly chosen 2-hour period. [4

	th month a company sells $X \log$ of brown sugar and $Y \log$ of white sugar, where X and Y have the ependent distributions $N(2500, 120^2)$ and $N(3700, 130^2)$ respectively.
(a)	Find the mean and standard deviation of the total amount of sugar that the company sells in 3 randomly chosen months.
	company makes a profit of \$1.50 per kilogram of brown sugar sold and makes a loss of \$0.20 per ogram of white sugar sold.
(b)	Find the probability that, in a randomly chosen month, the total profit is less than \$3000. [5]

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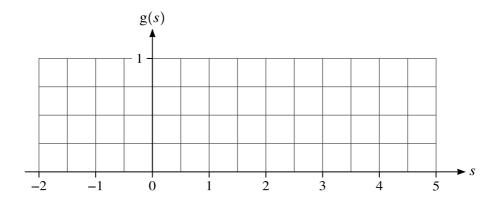
1)	The masses of size A stones have standard deviation 6 grams. The mean mass of a random sar of 200 size A stones is 45 grams.	nple
	Find a 95% confidence interval for the population mean mass of size A stones.	[3
		••••
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)	The masses of size B stones have standard deviation 11 grams. Using a random sample of size	200
,	an $\alpha\%$ confidence interval for the population mean mass is found to have width 4 grams.	200
•)		
	an $\alpha\%$ confidence interval for the population mean mass is found to have width 4 grams.	
•)	an $\alpha\%$ confidence interval for the population mean mass is found to have width 4 grams.	
-)	an $\alpha\%$ confidence interval for the population mean mass is found to have width 4 grams.	[4]
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	an $\alpha\%$ confidence interval for the population mean mass is found to have width 4 grams.	[4]
	an $\alpha\%$ confidence interval for the population mean mass is found to have width 4 grams. Find α .	[4]
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The diagram shows the graph of the probability density function of a random variable X that takes values between -1 and 3 only. It is given that the graph is symmetrical about the line x = 1. Between x = -1 and x = 3 the graph is a quadratic curve.

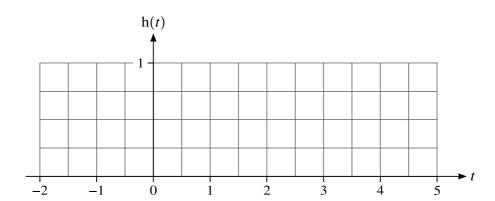
The random variable *S* is such that $E(S) = 2 \times E(X)$ and Var(S) = Var(X).

(a) On the grid below, sketch a quadratic graph for the probability density function of S. [1]



The random variable *T* is such that E(T) = E(X) and $Var(T) = \frac{1}{4}Var(X)$.

(b) On the grid below, sketch a quadratic graph for the probability density function of T. [2]



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It is now given that

$$f(x) = \begin{cases} \frac{3}{32}(3 + 2x - x^2) & -1 \le x \le 3, \\ 0 & \text{otherwise.} \end{cases}$$

•	Given that $P(1 - a < X < 1 + a) = 0.5$, show that $a^3 - 12a + 8 = 0$.	
I	Hence verify that $0.69 < a < 0.70$.	

She is 31	.8 minutes. You should assume that the standard deviation is unchanged.
(a)	Carry out a hypothesis test, at the 8% significance level, of whether Laxmi's mean journey time has decreased. [5]

Later Laxmi carries out a similar test with the same hypotheses, at the 8% significance level, using another random sample of size 50.

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