## Cambridge IGCSE ${ }^{\text {TM }}$



CENTRE NUMBER


## MATHEMATICS

0580/33
Paper 3 (Core)
May/June 2023
2 hours
You must answer on the question paper.
You will need: Geometrical instruments

## INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- For $\pi$, use either your calculator value or 3.142 .


## INFORMATION

- The total mark for this paper is 104.
- The number of marks for each question or part question is shown in brackets [ ].

1 (a) Claudia asks some students to choose their favourite science from biology, chemistry and physics. The pie chart shows the results.

(i) Find the percentage of students who choose chemistry.
$\qquad$
(ii) Find the fraction of students who choose physics.

Give your answer in its simplest form.
$\qquad$
(iii) For the number of students choosing each subject, find the ratio biology : chemistry : physics. Give your answer in its simplest form.
$\qquad$
$\qquad$ :
(iv) Marcus says:
'I do not know how many people choose chemistry, but I do know it is an even number.'
Explain how Marcus knows this.
$\qquad$
(v) Claudia now tells Marcus that 26 students choose chemistry.

Work out how many students choose physics.
(b) The Venn diagram shows information about the number of students in a class who study geography $(G)$ and history $(H)$.

(i) Work out the number of students in the class.
$\qquad$
(ii) Find $\mathrm{n}(G)$.
$\qquad$
(iii) One of the students is chosen at random.

Find the probability that this student studies geography and history.
$\qquad$
(iv) One of the students who studies geography and history stops studying history.

Complete this Venn diagram to show this change.


2 A shop sells food and drink.
(a) Bananas cost $\$ 1.20$ per kilogram and apples cost $\$ 2.25$ per bag.

Work out the total cost of 3.5 kg of bananas and 2 bags of apples.
\$
(b) Students receive a $10 \%$ discount on their shopping.

Before the discount, the cost of a student's shopping is $\$ 16.80$.
Work out the amount of the discount.
\$
(c) The cost of a cabbage increases by $15 \%$.

Calculate the new price if the original price is $\$ 1.80$.
\$
(d) Some customers have their shopping delivered to their home.

The cost is $\$ 5$ plus $\$ 1.50$ for each kilometre travelled from the shop to their home.
(i) Show that the cost for a customer living 10 km from the shop is $\$ 20$.
(ii)


On the grid, draw a line to show the cost of having shopping delivered.
(e) A bottle of water costs $\$ 1.55$.

Suki has \$20.

Work out the maximum number of bottles Suki can buy and the change she receives.

Maximum number of bottles $\qquad$
Change \$
(f) A farmer delivers eggs to the shop in trays of 50.

The eggs are then put into boxes of 12 .
There are no eggs left in the trays and all of the egg boxes are full.
Work out the smallest possible number of eggs that the farmer delivers.
$\qquad$
(g) The shop sells bottles of orange juice in three different sizes.

| Bottle A | Bottle B | Bottle C |
| :---: | :---: | :---: |
| 0.5 litres | 1.2 litres | 2 litres |
| $\$ 1.30$ | $\$ 3.20$ | $\$ 5.25$ |

Work out which bottle is the best value.
Show how you decide.

Bottle

3 (a) The diagram shows a shape on a $1 \mathrm{~cm}^{2}$ grid.


Work out the area of the shape.
$\qquad$ $\mathrm{cm}^{2}$
(b)


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Work out the perimeter of the rectangle.
$\qquad$
(c) A square has an area of $841 \mathrm{~cm}^{2}$.

Work out the length of one side of the square.
$\qquad$
(d) The diagram shows a cuboid made from $1 \mathrm{~cm}^{3}$ cubes.


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(i) Work out the volume of the cuboid.
$\qquad$ $\mathrm{cm}^{3}$
(ii) Write down the dimensions of a different cuboid that can be made using all of the cubes.
$\qquad$
$\qquad$ .cm by
(e)


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The diagram shows three small circles and one large circle.
The large circle has radius 20 cm .
The small circles each have radius 4 cm .
Work out the shaded area.
Give your answer in terms of $\pi$.
$\qquad$ $\mathrm{cm}^{2}$
(f) The exterior angle of a 9-sided regular polygon is $40^{\circ}$.
(i) Work out the size of the interior angle of this polygon.
$\qquad$
(ii)


The diagram shows a regular pentagon inside part of a regular 9-sided polygon.
Work out the value of $x$.

$$
\begin{equation*}
x= \tag{4}
\end{equation*}
$$

4 (a) A boat sails from $A$ to $B$.
The travel graph shows this journey.

(i) Write down the time that the boat leaves $A$.
(ii) Work out how long, in minutes, it takes the boat to sail from $A$ to $B$.
$\qquad$ min [
(iii) The boat stays at $B$ for 20 minutes.

The boat then sails to $C$ at a constant speed of $8 \mathrm{~km} / \mathrm{h}$.
Complete the travel graph.
(iv) Work out the average speed, in $\mathrm{km} / \mathrm{h}$, for the whole journey from $A$ to $C$.
(b) The scale drawing shows the positions of two ports, $X$ and $Y$. The scale is 1 cm represents 8 km .

(i) Measure the bearing of $Y$ from $X$.
(ii) A boat, $B$, is 52 km from $X$ and 80 km from $Y$.

On the scale drawing, mark the position of $B$.
(iii) A ship, $S$, is on a bearing of $284^{\circ}$ from $X$.

Work out the bearing of $X$ from $S$.

5 The grid shows the first three diagrams in a sequence.
Each diagram is made using sticks.

(a) On the grid, draw Diagram 4.


Diagram 4
(b) Complete the table.

| Diagram number | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of sticks | 5 | 9 | 13 |  |  |

(c) (i) Find an expression, in terms of $n$, for the number of sticks in Diagram $n$.
(ii) One of the diagrams has 73 sticks.

Work out its Diagram number.

Diagram
(d) (i) Show that the total number of sticks needed to make the first 3 diagrams is 27 .
(ii) The total number of sticks needed to make the first $k$ diagrams is $2 k^{2}+3 k$.

Show that this expression gives the correct total number of sticks needed to make the first 3 diagrams.
(iii) Tobias wants to make the first 10 diagrams.

He has already made the first 3 diagrams.
He has 240 sticks left to make the remaining 7 diagrams.
Work out how many sticks he has left when all 10 diagrams are made.

(a) Write down the equation of line $L$ in the form $y=m x+c$.

$$
\begin{equation*}
y= \tag{2}
\end{equation*}
$$

(b) (i) Complete the table of values for $y=x^{2}-3 x-3$.

| $x$ | -2 | -1 | 0 | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ |  | 1 |  | -5 | -5 |  | 1 |  |

(ii) On the grid, draw the graph of $y=x^{2}-3 x-3$ for $-2 \leqslant x \leqslant 5$.
(c) (i) Write down the coordinates of the lowest point of the graph of $y=x^{2}-3 x-3$.
$\qquad$
(ii) On the grid, draw the line of symmetry of the graph of $y=x^{2}-3 x-3$.
(iii) Write down the equation of the line of symmetry.
(d) Write down the coordinates of the point where line $L$ intersects the graph of $y=x^{2}-3 x-3$ for $x>0$.
$\qquad$

7 (a)


The diagram shows a triangle $A B C$ and a straight line $B C D$.
(i) Angle $A C B=108^{\circ}$.

Write down the mathematical name for this type of angle.
$\qquad$
(ii) Work out the value of $x$.

$$
\begin{equation*}
x= \tag{1}
\end{equation*}
$$

(iii) Work out the value of $y$.

$$
\begin{equation*}
y= \tag{1}
\end{equation*}
$$

(b) Show that the mean of the angles in any triangle is $60^{\circ}$.
(c)


The diagram shows a right-angled triangle.
Calculate the value of $h$.

$$
h=
$$

(d)


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Triangle $A B C$ is similar to triangle $P Q R$.
(i) Calculate $P R$.

$$
P R=
$$

(ii) Calculate $B C$.

$$
B C=
$$

(e)


The diagram shows a right-angled triangle.
Calculate the perimeter of this triangle.

8 (a) The length, $l \mathrm{~m}$, of a piece of wire is 18.7 metres, correct to the nearest 10 centimetres.
Complete the statement about the value of $l$.
$\qquad$
(b) 850 metres of wire has a mass of 130.5 kilograms.

Work out the length of wire, in metres, that has a mass of 900 grams.
$\qquad$ m [3]
(c) Aluminium is used to make the wire.

The mass of $1 \mathrm{~cm}^{3}$ of aluminium is 2.7 grams.
Work out the mass, in grams, of $6000 \mathrm{~cm}^{3}$ of aluminium. Give your answer in standard form.
(d) A 12 metre length of wire increases in length to 12.017 metres when its temperature rises.

Calculate the percentage increase in the length of the wire.

